INDIAN INSTITUTE OF TECHNOLOGY TIRUPATI DEPARTMENT OF MATHEMATICS AND STATISTICS

MA635P-Scientific Programming Laboratory

Lab Exercise-4 (30 Marks) Deadline: 30 January 2025, 5:00 PM

- 1. Create an algorithm for Lagrange's interpolation method. [2.5]
- 2. Create an algorithm for Hermite's interpolation method. [2.5]
- 3. Write a Python code for the developed algorithm for Lagrange's interpolation and ε_t and test all examples of Lecture 10 and 11. [5]
- 4. Based on an experiment on heated plate, temperatures are measured at various points as given in below table. Estimate the temperature at (x, y) = (4, 3.2) and (x, y) = (4.3, 2.7) using Lagrange's interpolating polynomial $P_4(x)$. [5]

| y | x = 0 | x = 2 | x = 4 | x = 6 | x = 8 |
|---|-------|-------|-------|-------|-------|
| 0 | 100 | 90 | 80 | 70 | 60 |
| 2 | 85 | 64.49 | 53.5 | 48.15 | 50 |
| 4 | 70 | 48.9 | 38.43 | 35.03 | 40 |
| 6 | 55 | 38.78 | 30.39 | 27.07 | 30 |
| 8 | 40 | 35 | 30 | 25 | 20 |

- 5. Write a Python code for the developed algorithm for Hermite interpolation test the example given in Lecture 12. [5]
- 6. Draw your hand in a piece of paper as instructions given in the class and get (x_i, y_i) at 20 locations from your graph. Use Newton's divided difference or Lagrange interpolation or Hermite interpolation to recreate the graph with as much smooth as possible accuracy. Observe the irregular hand-shape in the drawing and suggest any remedy for this. [10]