MA635P-Scientific Programming Laboratory Padé Approximation

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Deadline: March 16, 2025







Padé Approximation

Title of the Project

Padé Approximation for Geophysics



Background

- A powerful technique for approximating functions using rational functions (fractions of polynomials).
- It often outperforms Taylor series and other polynomial approximations
- Taylor series expansions can diverge or converge very slowly for some functions (e.g., near singularities or for large xx).
- Padé approximants can provide better accuracy with fewer terms by capturing asymptotic behavior more effectively.
- It helps in numerical reconstructions in Medical Imaging and Signal Processing
- It can approximate activation functions like sigmoid and tanh more efficiently in ML.



Objective

- To explore how Padé approximants can be used to improve function approximations in numerical computing and machine learning applications.
- To focus on comparing Padé approximants with Taylor series, polynomial interpolation for different types of functions.



Requirements

Read the following papers:

- 1. Applications of Pade Approximation in Numerical Analysis
- 2. Rational Approximants Defined from Double Power Series



Steps to Solve

- 1. Construct Pade approximation for e^x
- 2. Check how does scipy does the pade approximation
- 1. Develop a Pade approximation for general function



Deliverable

- 1. A Python-code for Pade approximations
- 2. Visualizations of the numerical interpolation for the Pade approximation
- 3. Identify a problem that has the application of Pade approximation, For example Geophysics





Team

Team

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Thanks

Doubts and Suggestions

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