INDIAN INSTITUTE OF TECHNOLOGY TIRUPATI DEPARTMENT OF MATHEMATICS AND STATISTICS

Project - 1 MA517M-Basic Programming Laboratory Last Date: 09 November 2025 Name Roll No.: MA25M005

Hypergeometric Distribution using C++ Classes and Operator Overloading

Objective: To design a C++ program that implements the hypergeometric distribution using classes, computes PMF, CDF, expectation, variance, and supports operator overloading for comparison.

A hypergeometric random variable $X \sim \text{Hypergeom}(N, K, n)$ counts the number of successes in n draws without replacement from a population of size N containing K successes.

The probability mass function (PMF) is

$$P(X=k) = \frac{\binom{K}{k} \binom{N-K}{n-k}}{\binom{N}{n}}, \quad \max(0, n+K-N) \le k \le \min(K, n)$$

Mean and variance:

$$\mathbb{E}[X] = n \frac{K}{N}, \quad \text{Var}(X) = n \frac{K}{N} \frac{N - K}{N} \frac{N - n}{N - 1}$$

Problem Description

Design a class Hypergeometric RV to represent a hypergeometric random variable. The class should allow computation of PMF, CDF, mean, variance, and comparison with other hypergeometric random variables using operator overloading.

Class Specification

- Class Name: HypergeometricRV
- Private Data Members:
 - int N;
 - int K;
 - int n;
- Public Member Functions:
 - HypergeometricRV(int population, int success, int draws);
 - double pmf(int k) const;
 - double cdf(int k) const;
 - double mean() const;
 - double variance() const;
 - void display() const;

Operator Overloading

- operator ==(), !=(), <(), >() Compares mean or variance of two hypergeometric random variables
- operator <<() Displays the hypergeometric variable's parameters and statistics

Tasks

- 1. Create a hypergeometric random variable $X \sim \text{Hypergeom}(N=50, K=10, n=5)$
- 2. Compute PMF and CDF for selected values of k
- 3. Compute mean and variance
- 4. Create another variable $Y \sim \text{Hypergeom}(50, 15, 5)$ and compare X and Y
- 5. Display results using the overloaded << operator

Expected Output Example

```
X ~ Hypergeom(N=50, K=10, n=5)
PMF P(X=2) = 0.275
CDF P(X<=2) = 0.678
Mean = 1.0, Variance = 0.796
Y ~ Hypergeom(N=50, K=15, n=5)
Mean = 1.5, Variance = 0.983
X < Y : True
X == Y: False</pre>
```

Project - 2: Lights Out Game Using C++ Classes

Problem Statement

Design and implement the **Lights Out Game** using **C++ classes**. The game consists of a grid of lights, where each light can be either *on* or *off*. Pressing a light toggles its state and the state of its adjacent neighbors (up, down, left, right). The objective is to turn all lights off. The project should utilize object-oriented programming concepts such as classes, objects, encapsulation, and methods for handling grid updates and game logic.

Project Requirements

- 1. Create a Light class to represent a single light in the grid.
 - (a) Data member: current state (on/off)
 - (b) Methods: toggle(), getState()
- 2. Create a Grid class to represent the game board.

- (a) Initialize the grid with a random pattern of lights on and off.
- (b) Display the current state of the grid in a readable format.
- (c) Toggle a selected light and its adjacent neighbors when a user chooses a cell.
- (d) Include a method to check if all lights are off (win condition).
- 3. Create a Game class to manage gameplay.
 - (a) Display options for the user: Play or Solution.
 - (b) If the user chooses Play, allow them to select lights to toggle.
 - (c) Allow the user to quit and confirm before exiting.
 - (d) Optionally, allow the user to reset the board or play multiple rounds.
- 4. Ensure proper encapsulation of light and grid operations within the respective classes.

Suggested Class Structure

- 1. Light Class:
 - Data member: bool isOn
 - Methods: toggle(), getState()
- 2. Grid Class:
 - Data member: 2D array of Light objects
 - Methods: initializeGrid(), displayGrid(), toggleLight(int row, int col), isWin()
- 3. Game Class:
 - Data member: Grid object, user choice, move counter
 - Methods: playGame(), showSolution(), confirmQuit(), resetBoard()

Reference

For more details about the Lights Out game, visit: https://en.wikipedia.org/wiki/Lights_Out_ (game)