INDIAN INSTITUTE OF TECHNOLOGY TIRUPATI DEPARTMENT OF MATHEMATICS AND STATISTICS

Project - 1 MA517M-Basic Programming Laboratory Last Date: 09 November 2025 Name Roll No.: MA25M019

Quaternion Arithmetic using C++ Classes and Operator Overloading

Objective: To design a C++ program that implements quaternions using classes, supports arithmetic operations, and demonstrates operator overloading.

A quaternion is an extension of complex numbers:

$$q = a + b i + c j + d k$$

where $a, b, c, d \in \mathbb{R}$, and i, j, k satisfy

$$i^2 = j^2 = k^2 = ijk = -1, \quad ij = k, \ ji = -k, \dots$$

Quaternions are used in 3D rotations and physics, and their multiplication is non-commutative.

Problem Description

Design a class Quaternion that represents quaternions. The class should support addition, subtraction, multiplication, division (by the norm squared), conjugation, and equality comparison using operator overloading.

Class Specification

- Class Name: Quaternion
- Private Data Members:
 - double a, b, c, d; // real and imaginary components
- Public Member Functions:
 - Quaternion(double a=0, double b=0, double c=0, double d=0); Constructor initializes the quaternion
 - double norm() const; Computes $||q|| = \sqrt{a^2 + b^2 + c^2 + d^2}$
 - Quaternion conjugate() const; Returns $\bar{q} = a bi cj dk$
 - void display() const; Displays quaternion in a + bi + cj + dk form

Operator Overloading

- operator +(), -() Addition and subtraction component-wise
- operator *() Quaternion multiplication using the rules:

$$ij = k$$
, $ji = -k$, $jk = i$,...

- operator /() Division using inverse: $q_1/q_2 = q_1 * q_2^{-1}$
- operator ==() Checks the equality of two quaternions

Tasks

- 1. Create quaternions $q_1 = 1 + 2i + 3j + 4k$ and $q_2 = 2 i + k$
- 2. Compute $q_1 + q_2$, $q_1 q_2$, $q_1 * q_2$, q_1/q_2
- 3. Compute norms and conjugates of q_1 and q_2
- 4. Compare q_1 and q_2 using equality operator

Expected Output Example

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\begin{array}{l} q1 = 1 + 2i + 3j + 4k \\ q2 = 2 - i + 0j + 1k \\ \\ q1 + q2 = 3 + 1i + 3j + 5k \\ q1 - q2 = -1 + 3i + 3j + 3k \\ q1 * q2 = -12 + 4i + 10j + 4k \\ q1 / q2 = 0.44 + 1.11i + 0.67j + 0.22k \\ \\ \\ \text{Norm of } q1 = 5.477 \\ \\ \text{Conjugate of } q1 = 1 - 2i - 3j - 4k \\ \end{array}
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Project - 2: Conway's Game of Life Using C++ Classes

Problem Statement

q1 == q2 : False

Design and implement Conway's Game of Life using C++ classes. This is a zero-player game where the evolution of a 2D grid is determined by its initial state and simple rules. Each cell in the grid can be *alive* or *dead*, and the next generation of the grid is calculated based on the number of alive neighbors. The project should utilize object-oriented programming concepts such as classes, objects, encapsulation, and methods for handling game logic and grid updates.

Project Requirements

- 1. Create a Cell class to represent a single cell in the grid.
 - (a) Data member: current state (alive or dead)
 - (b) Methods: setState(), getState()
- 2. Create a Grid class to represent the game board (matrix).
 - (a) Initialize the grid with random alive and dead cells.
 - (b) Include a method to display the current state of the grid.
 - (c) Include a method to count alive neighbors for each cell.
 - (d) Include a method to update the grid according to the following rules:
 - Any live cell with fewer than two live neighbors dies (underpopulation).
 - Any live cell with two or three live neighbors lives on.
 - Any live cell with more than three live neighbors dies (overpopulation).
 - Any dead cell with exactly three live neighbors becomes alive (reproduction).
- 3. Create a Game class to manage simulation.
 - (a) Display options for the user: Start, Next Generation, or Quit.
 - (b) Allow the user to advance the simulation one generation at a time.
 - (c) Allow the user to quit and confirm before exiting.
 - (d) Optionally, allow the user to specify the number of generations to simulate automatically.
- 4. Ensure proper encapsulation of cell and grid operations within the respective classes.

Suggested Class Structure

- 1. Cell Class:
 - Data member: bool isAlive
 - Methods: setState(bool state), getState()
- 2. Grid Class:
 - Data member: 2D array of Cell objects
 - Methods: initializeGrid(), displayGrid(), countAliveNeighbors(int row, int col), update-Grid()
- 3. Game Class:
 - Data member: Grid object, user choice, generation counter
 - Methods: startGame(), nextGeneration(), confirmQuit()

Reference

For more details about Conway's Game of Life, visit: https://en.wikipedia.org/wiki/Conway's_Game_of_Life